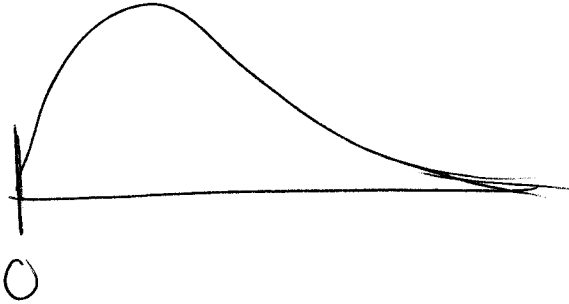


# Key

## Chapter 9 Review Chi Squared Distributions

What does a  $\chi^2$  distribution look like?

a. DRAW:



b. Describe the shape:

- rt. skewed
- center @ ?
- spread  $0 \rightarrow \infty$

How many  $\chi^2$  distributions are there?

infinitely many - based on sample size

Like the t-distribution, what do we ALWAYS have to include with the p-value for a  $\chi^2$  test of significance?

df!

What is different about the hypotheses for a  $\chi^2$  test of significance?

- written out
- full sentences
- no #'s
- always "two-sided" (no  $>$  or  $<$  alt.)

## $\chi^2$ Goodness of Fit Test

What type of data is this test done on?

one-var. distribution (list of data) <sup>categories -</sup>

What are we trying to assess?

whether the observed distr. (from sample, expt) fits expected (from pop.)

Hypotheses:  $H_0$ : the observed freq. distribution of (context) fits the expected distribution

$H_a$ : " " " " " doesn't fit

Test Statistic:  $\chi^2 = \sum \frac{(obs - exp)^2}{exp} = \frac{(\quad)^2}{\quad} + \frac{(\quad)^2}{\quad} + \dots = \text{test stat}$

P-value:  $P(\chi^2 > \text{test stat} \mid df = \quad) = \quad$   
 $df = k - 1$  (# categories - 1)

Conclusion: We reject/fail to reject.....  $H_0$ ...

We have suff. evidence that... (re-copy  $H_0$  or  $H_a$ )

Assumptions: 1) SRS

2) large  $n$  so that all expected counts  $\geq 5$

On calculator:

$L_1 = \text{obs.}$

$L_2 = \text{exp.}$

$L_3 = (L_1 - L_2)^2 / L_2$

$\text{sum}(L_3) = \chi^2$

P-val:  $\chi^2 \text{cdf}(\text{LB}, \text{UB}, df)$   
 $\uparrow \quad \uparrow$   
test stat  $\epsilon_{99}$

### Example: #1

In a recent year, at the 6 P.M. time slot, television channels 3, 6, 10, and 29 captured the entire audience with 30%, 25%, 20%, and 25%, respectively. During the first week of the next season, 500 viewers are interviewed.

- a. If viewer preferences have not changed, what number of persons is expected to watch each channel?

state  
1) SRS  
2) all expected counts  $\geq 5$   
check  
1) assumed  $\checkmark$

| Channel | exp | obs |
|---------|-----|-----|
| 3       | 150 | 139 |
| 6       | 125 | 138 |
| 10      | 100 | 112 |
| 29      | 125 | 111 |

- b. If the actual observed values are 139, 138, 112, and 111, is there a significant difference?

$H_0$ : the observed freq. distrib. of TV channels fits the expected distrib.

$H_a$ : the observed freq. distrib. of TV channels doesn't fit the expected distrib.

$$\chi^2 = \sum \frac{(\text{obs} - \text{exp})^2}{\text{exp}} = \frac{(139 - 150)^2}{150} + \frac{(138 - 125)^2}{125} + \dots = 5.1667$$

$$P(\chi^2 > 5.1667 / df = 3) = 0.16$$

- We fail to reject  $H_0$  b/c p-value  $> \alpha = 0.05$ .
- We have sufficient evidence that....  
(re-copy  $H_0$ ).

## $\chi^2$ Test for Association

What type of data is this test done on?

2 var. distribution (2 way table)

What are we trying to assess?

• whether obs fits expected distr.

How do we find the expected cell counts for a table of data?

$$\text{exp. counts} = \frac{\text{row total} \times \text{column total}}{n}$$

Hypotheses:  $H_0$ : there is no association btw. row var. and column var., (they are indep)

$H_a$ : there is an assoc. btw. ....  
(they are dependent)

Test Statistic:  $\chi^2 = \sum \frac{(\text{obs} - \text{exp})^2}{\text{exp}} = \frac{(\quad)^2}{\quad} + \frac{(\quad)^2}{\quad} + \dots = \text{test stat}$

P-value:  $P(\chi^2 > \text{test stat} \mid \text{df} = \quad) =$

$$\text{df} = (r-1)(c-1)$$

Conclusion: We reject/fail to reject.....

We have suff. evidence that... re-copy  $H_0/H_a$

Assumptions: 1) 2 indep. SKS

2) large enough  $n$  so all exp. counts  $\geq 5$

On calculator:

- put data into matrix [A]

- Use  $\chi^2$  test

- expected are put into [B] by calculator

Example:

The following table is from the July 1993 publication of *Vital and Health Statistics* from the Centers for Disease Control and Prevention/National Center for Health Statistics. The individuals in the following table have only one of the three indicated irritations.

| Irritation | 18-29 | 30-44 | 45-64 | 65+ | total |
|------------|-------|-------|-------|-----|-------|
| Eye        | 440   | 567   | 349   | 59  | 1415  |
| Nose       | 924   | 1311  | 794   | 102 | 3131  |
| Throat     | 253   | 311   | 157   | 19  | 740   |
| total      | 1617  | 2189  | 1300  | 180 | 5286  |

State

2 indep.

1) SRS

2) all exp. cants  $\geq 5$

Check

1) assumed

2) ✓

a. How many rows are there in the table above?

3

b. How many cells are there?

12

c. How many columns are there?

4

d. What is the df?

$(3-1)(4-1) = 6$

e. Determine if the type of irritation is independent of the age group using a 0.05 level of significance.

H0: irritation + age are independent

Ha: " " " dependent

$$\chi^2 = \sum \frac{(obs - exp)^2}{exp} = \frac{(440 - 432.85)^2}{432.85} + \frac{(567 - 585.97)^2}{585.97} + \dots = 13.619$$

$$P(\chi \geq 13.619 | df=6) = 0.034$$

We reject H0 b/c p-value <  $\alpha = 0.05$ .

~~dependent~~

We have sufficient evidence that irritation + age are dependent.